Introduction to Three Dimensional Geometry

Exercise 11.1

Ouestion 1:

A point is on the x-axis. What are its y-coordinate and z-coordinates?

Solution:

If a point is on the x-axis, then the coordinates of y and z are 0. So, the point is (x,0,0).

Question 2:

A point is in the XZ – plane. What can you say about its y – coordinate?

Solution:

If a point is in XZ – plane, then its y – coordinate is 0.

Question 3:

Name the octants in which the following points lie:

$$(1,2,3), (4,-2,3), (4,-2,-5), (4,2,-5), (-4,2,-5), (-4,2,5), (-3,-1,6), (2,-4,-7).$$

Solution:

Here is the table which represents the octants:

Octants	I	II	III	IV	V	VI	VII	VIII
X	+	_		+	+	_	_	+
y	+	+	- 4	_	+	+	_	_
z	+	+	+	+	_	_	_	_

- (i) (1,2,3) Here x is positive, y is positive, and z is positive. So, it lies in I octant.
- (ii) (4,-2,3)Here x is positive, y is negative, and z is positive. So, it lies in IV octant.
- (iii) (4,-2,-5)Here x is positive, y is negative, and z is negative. So, it lies in VIII octant.

- (iv) (4,2,-5)Here x is positive, y is positive, and z is negative. So, it lies in V octant.
- (v) (-4,2,-5)Here x is negative, y is positive, and z is negative. So, it lies in VI octant.
- (vi) (-4,2,5)Here x is negative, y is positive, and z is positive. So, it lies in II octant.
- (vii) (-3,-1,6)Here x is negative, y is negative, and z is positive. So, it lies in III octant.
- (viii) (2,-4,-7)Here x is positive, y is negative, and z is negative. So, it lies in VIII octant.

Question 4:

Fill in the blanks:

- (i) The x-axis and y-axis taken together determine a plane known as XY plane.
- (ii) The coordinates of points in the XY-plane are of the form (x, y, 0).
- (iii) Coordinate planes divide the space into eight octants.