# Question 1 :

Monthly consumption (in units)	Number of consumers
65 - 85	4
85 - 105	5
105 - 125	13
125 - 145	20
145 - 165	14
165 - 185	8
185 - 205	4

The following frequency distribution gives the monthly consumption of electricity of 68 consumers of a locality. Find the median, mean and mode of the data and compare them.

### Answer :

To find the class marks, the following relation is used.

 $Class mark = \frac{Upper class limit + Lower class limit}{2}$ 

Taking 135 as assumed mean (*a*), *d<sub>i</sub>*, *u<sub>i</sub>*, *f<sub>i</sub>u<sub>i</sub>* are calculated according to step deviation method as follows.

Monthly consumption (in units)	Number of consumers (f i)	<i>x:</i> class mark	$d_i = x_i - 135$	$u_i=\frac{d_i}{20}$	f <sub>i</sub> u <sub>i</sub>
65 - 85	4	75	- 60	- 3	- 12
85 - 105	5	95	- 40	- 2	- 10
105 - 125	13	115	- 20	- 1	- 13
125 - 145	20	135	0	0	0
145 - 165	14	155	20	1	14

165 - 185	8	175	40	2	16
185 - 205	4	195	60	3	12
Total	68				7

From the table, we obtain

$$\sum f_i u_i = 7$$
$$\sum f_i = 68$$

Class size (h) = 20

Mean, 
$$\overline{x} = a + \left(\frac{\sum f_i u_i}{\sum f_i}\right) \times h$$
  
=  $135 + \frac{7}{68} \times 20$   
=  $135 + \frac{140}{68}$   
=  $137.058$ 

From the table, it can be observed that the maximum class frequency is 20, belonging to class interval 125 - 145.

Modal class = 125 - 145

Lower limit (*I*) of modal class = 125

Class size (h) = 20

Frequency  $(f_1)$  of modal class = 20

Frequency ( $f_0$ ) of class preceding modal class = 13 Frequency

 $(f_2)$  of class succeeding the modal cla

## **Question2**:

Class interval	Frequency
0 - 10	5
10 - 20	x
20 - 30	20
30 - 40	15
40 - 50	у
50 - 60	5
Total	60

### Answer :

The cumulative frequency for the given data is calculated as follows.

Class interval	Frequency	Cumulative frequency
0 - 10	5	5
10 - 20	x	5+x
20 - 30	20	25 + x
30 - 40	15	40 + x
40 - 50	У	40 + x + y
50 - 60	5	45 + x + y
Total (n)	60	

From the table, it can be observed that n = 60

45 + x + y = 60 x

$$+ y = 15(1)$$

Median of the data is given as 28.5 which lies in interval 20 - 30.

Therefore, median class = 20 - 30

Lower limit (I) of median class = 20

Cumulative frequency (*cf*) of class preceding the median class = 5 + x

Frequency (f) of median class = 20

Class size (h) = 10

Median = 
$$l + \left(\frac{\frac{n}{2} - cf}{f}\right) \times h$$
  

$$28.5 = 20 + \left[\frac{\frac{60}{2} - (5+x)}{20}\right] \times 10$$

$$(25 - x)$$

$$8.5 = \left(\frac{25-x}{2}\right)$$
$$17 = 25-x$$

$$x = 8$$

From equation (1),

$$8 + y = 15 y = 7$$

Hence, the values of x and y are 8 and 7 respectively.

# Question3 :

A life insurance agent found the following data for distribution of ages of 100 policy holders. Calculate the median age, if policies are given only to persons having age 18 years onwards but less than 60 year.

Age (in years)	Number of policy holders
Below 20	2
Below 25	6
Below 30	24
Below 35	45
Below 40	78
Below 45	89

Below 50	92
Below 55	98
Below 60	100

### Answer :

Here, class width is not the same. There is no requirement of adjusting the frequencies according to class intervals. The given frequency table is of less than type represented with upper class limits. The policies were given only to persons with age 18 years onwards but less than 60 years. Therefore, class intervals with their respective cumulative frequency can be defined as below.

Age (in years)	Number of policy holders $(f_i)$	Cumulative frequency (cf)
18 - 20	2	2
20 - 25	6 - 2 = 4	6
25 - 30	24 - 6 = 18	24
30 - 35	45 - 24 = 21	45
35 - 40	78 - 45 = 33	78
40 - 45	89 - 78 = 11	89
45 - 50	92 - 89 = 3	92
50 - 55	98 - 92 = 6	98
55 - 60	100 - 98 = 2	100
Total (n)		

From the table, it can be observed that n = 100.

$$\frac{n}{2}$$
(i.e.,  $\frac{100}{2} = 50$ )

/ is 78, belonging to interval 35 - 40.

Cumulative frequency (*cf*) just greater than

Therefore, median class = 35 - 40

Lower limit (I) of median class = 35

Class size (h) = 5

Frequency (*t*) of median class = 33

Cumulative frequency (*cf*) of class preceding median class = 45

Median = 
$$l + \left(\frac{\frac{n}{2} - cf}{f}\right) \times h$$
  
=  $35 + \left(\frac{50 - 45}{33}\right) \times 5$   
=  $35 + \frac{25}{33}$   
=  $35.76$ 

Therefore, median age is 35.76 years.

## **Question 4**:

The lengths of 40 leaves of a plant are measured correct to the nearest millimeter, and the data obtained is represented in the following table:

Length (in mm)	Number or leaves fi
118 - 126	3
127 - 135	5
136 - 144	9
145 - 153	12
154 - 162	5
163 - 171	4
172 - 180	2

Find the median length of the leaves.

(Hint: The data needs to be converted to continuous classes for finding the median, since the formula assumes continuous classes. The classes then change to 117.5 - 126.5, 126.5 - 135.5... 171.5 - 180.5)

#### Answer :

The given data does not have continuous class intervals. It can be observed that the difference between two class

$$-=0.5$$

intervals is 1. Therefore, 2 has to be added and subtracted to upper class limits and lower class limits respectively.

Continuous class intervals with respective cumulative frequencies can be represented as follows.

Length (in mm)	Number or leaves <i>f</i> <sub>i</sub>	Cumulative frequency
117.5 - 126.5	3	3
126.5 - 135.5	5	3 + 5 = 8
135.5 - 144.5	9	8 + 9 = 17
144.5 - 153.5	12	17 + 12 = 29
153.5 - 162.5	5	29 + 5 = 34
162.5 - 171.5	4	34 + 4 = 38
171.5 - 180.5	2	38 + 2 = 40

$$\left(i.e., \frac{40}{2} = 20\right)_{is 29, is 29, is$$

n

From the table, it can be observed that the cumulative frequency just greater than 2

belonging to class interval 144.5 - 153.5. Median class = 144.5 - 153.5

Lower limit (I) of median class = 144.5

Class size (h) = 9

Frequency (f) of median class = 12

Cumulative frequency (*cf*) of class preceding median class = 17

$$=l+\left(rac{n}{2}-cf
ight)\times h$$

Median

$$= 144.5 + \left(\frac{20 - 17}{12}\right) \times 9$$
$$= 144.5 + \frac{9}{4} = 146.75$$

Therefore, median length of leaves is 146.75 mm.

# Question 5 :

Life time (in hours)	Number of lamps
1500 - 2000	14
2000 - 2500	56
2500 - 3000	60
3000 - 3500	86
3500 - 4000	74
4000 - 4500	62
4500 - 5000	48

## Find the following table gives the distribution of the life time of 400 neon lamps:

Find the median life time of a lamp.

## Answer :

Thecumulative frequencies with their respective class intervals are as follows.

Life time	Number of lamps (fi)	Cumulative frequency
1500 - 2000	14	14
2000 - 2500	56	14 + 56 = 70
2500 - 3000	60	70 + 60 = 130
3000 - 3500	86	130 + 86 = 216
3500 - 4000	74	216 + 74 = 290
4000 - 4500	62	290 + 62 = 352
4500 - 5000	48	352 + 48 = 400
Total ( <i>n</i> )	400	

It can be observed that the cumulative frequency just greater than interval 3000 - 3500.

$$\frac{n}{2}$$
 (i.e.,  $\frac{400}{2} = 200$ )

is 216, belonging to class

Median class = 3000 - 3500

Lower limit () of median class = 3000

Frequency (f) of median class = 86

Cumulative frequency (*cf*) of class preceding median class = 130

Class size (h) = 500

$$= l + \left(\frac{\frac{n}{2} - cf}{f}\right) \times h$$

Median

$$= 3000 + \left(\frac{200 - 130}{86}\right) \times 500$$
$$= 3000 + \frac{70 \times 500}{86}$$

= 3406.976

Therefore, median life time of lamps is 3406.98 hours.

## **Question 6 :**

100 surnames were randomly picked up from a local telephone directory and the frequency distribution of the number of letters in the English alphabets in the surnames was obtained as follows:

Number of letters	1 - 4	4 - 7	7 - 10	10 - 13	13 - 16	16 - 19
Number of surnames	6	30	40	6	4	4

Determine the median number of letters in the surnames. Find the mean number of letters in the surnames?

Also, find the modal size of the surnames.

## Answer :

The cumulative frequencies with their respective class intervals are as follows.

Number of letters	<b>Frequency</b> ( <i>f</i> <sub>i</sub> )	Cumulative frequency
1 - 4	6	6
4 - 7	30	30 + 6 = 36

7 - 10	40	36 + 40 = 76
10 - 13	16	76 + 16 = 92
13 - 16	4	92 + 4 = 96
16 - 19	4	96 + 4 = 100
Total ( <i>n</i> )	100	

 $\frac{n}{2}$  (i.e.,  $\frac{100}{2} = 50$ )

is 76, belonging to class

It can be observed that the cumulative frequency just greater than interval 7 - 10.

Median class = 7 - 10

Lower limit (I) of median class = 7

Cumulative frequency (cf) of class preceding median class = 36

Frequency (f) of median class = 40

Class size (h) = 3

$$=l+\left(rac{n}{2}-cf
ight)\times h$$

Median

$$= 7 + \left(\frac{50 - 36}{40}\right) \times 3$$
$$= 7 + \frac{14 \times 3}{40}$$

= 8.05

To find the class marks of the given class intervals, the following relation is used.

 $Class mark = \frac{Upper class limit + Lower class limit}{2}$ 

Number of letters	Number of surnames $f_i$	X	$d_i = x_i - 11.5$	$u_i = \frac{d_i}{3}$	f,u,
1 - 4	6	2.5	- 9	- 3	- 18
4 - 7	30	5.5	- 6	- 2	- 60
7 - 10	40	8.5	- 3	- 1	- 40
10 - 13	16				

Taking 11.5 as assumed mean (a), d<sub>ii</sub> u<sub>ii</sub> and f<sub>i</sub>u<sub>i</sub> are calculated according to step deviation method as follows.

# **Question 7**:

The distribution below gives the weights of 30 students of a class. Find the median weight of the students.

Weight (in kg)	40 - 45	45 - 50	50 - 55	55 - 60	60 - 65	65 - 70	70 - 75
Number of students	2	3	8	6	6	3	2

### Answer :

The cumulative frequencies with their respective class intervals are as follows.

Weight (in kg)	<b>Frequency</b> ( <i>fi</i> )	Cumulative frequency
40 - 45	2	2
45 - 50	3	2 + 3 = 5
50 - 55	8	5 + 8 = 13
55 - 60	6	13 + 6 = 19
60 - 65	6	19 + 6 = 25
65 - 70	3	25 + 3 = 28
70 - 75	2	28 + 2 = 30

u

Total ( <i>n</i> )	30	
Cumulative frequency just greater th	$\frac{n}{2}\left(\text{i.e., }\frac{30}{2}=15\right)$ is 19 below	onging to class interval 55 - 60
Median class – 55 - 60		
Lower limit ( $\Lambda$ of median class = 55		
Erequency (f) of median class = $6$		
Cumulative frequency (cf) of media	- dass - 13	
	101855 - 15	
$= l + \left(\frac{\frac{n}{2} - cf}{f}\right) \times h$ Median $= 55 + \left(\frac{15 - 13}{6}\right) \times 5$ $= 55 + \frac{10}{6}$ $= 56.67$		
Therefore, median weight is 56.67 k	.g.	