

Chapter 9: Differential Equations

Ex-9.1

Determine order and degree (if defined) of differential equations given in Questions 1 to 10:

Q1. $\frac{d^4 y}{dx^4} + \sin(y') = 0$

A.1. The highest order derivation present in the differential equation (D.E.) is $\frac{d^4 y}{dx^4}$, so its order is 4.

As, the given D.E. is not a polynomial equation in its derivative, its degree is not defined.

Q2. $y' + 5y = 0$

A.2. The highest order derivation present in the D.E. is y' , so its order is 1.

As the given D.E. is a polynomial equation in its derivative its degree is 1.

Q3. $\left(\frac{ds}{dt}\right)^4 + 3s \frac{d^2 s}{dt^2} = 0$

A.3. The highest order derivation present in the D.E. is $\frac{d^2 s}{dt^2}$ so its order is 2.

As the given D.E. is a polynomial equation in its derivative its degree is 1.

Q4. $\frac{d^2 y}{(dx^2)^2} + \cos\left(\frac{dy}{dx}\right) = 0$

A.4. $\frac{d^2 y}{(dx^2)^2}$ As the given D.E. is not a polynomial equation in its derivative, its degree is not defined.

Q5. $\frac{d^2 y}{dx^2} = \cos 3x + \sin 3x$

A.5. $\frac{d^2 y}{dx^2}$ As the given D.E. is a polynomial equation in its derivative, its degree is 1.

Q6. $(y''') + (y'') + (y')^4 + y^5 = 0$

A.6. The highest order derivative present in the D.E. is y''' so its order is 3.

As the given D.E. is a polynomial equation in its derivative, its degree is 2.

Q7. $y''' + 2y'' + y' = 0$

A.7. The highest order present in the D.E. is y''' so its order is 3.

As the given D.E. is a polynomial equation in its derivative, its degree is 1.

Q8. $y' + y = e^x$

A.8. The given order derivative present in the D.E. is y' so its order is 1.

As the given D.E. is a polynomial equation in its derivative, its degree is 1.

Q9. $y'' + (y')^2 + 2y = 0$

A.9. The highest order derivative present in the D.E. is y'' so its order is 2.

As the given D.E. is a polynomial equation in its derivative, its degree is 1.

Q10. $y'' + 2y' + \sin y = 0$

A.10. The highest order derivative present in the D.E. is y'' so its order is 2.

As the given D.E. is polynomial equation in its derivative, its degree is 1.

Q11. The degree of the differential equation $\left(\frac{d^2y}{dx^2}\right)^3 + \left(\frac{dy}{dx}\right)^2 + \sin\left(\frac{dy}{dx}\right) + 1 = 0$ is:

(A) 3

(B) 2

(C) 1

(D) Not defined

A.11. In the given D.E,

$\sin \frac{dy}{dx}$ is a trigonometric function of derivative $\frac{dy}{dx}$. So it is not a polynomial equation so its derivative is not defined.

Hence, Degree of the given D.E. is not defined.

$\therefore$ Option (D) is correct.

Q12. The order of the differential equation $2x^2 \frac{d^2 y}{dx^2} - 3 \frac{dy}{dx} + y = 0$ is:

(A) 2

(B) 1

(C) 0

(D) Not defined

A.12. The highest order derivative present in the given D.E. is $\frac{d^2 y}{dx^2}$ and its order is 2.

$\therefore$ Option (A) is correct.